

VAPOR PRESSURE AND VISCOSITY

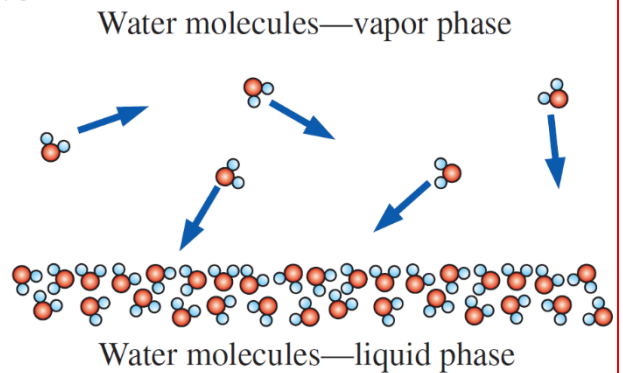
In this lesson, we will:

- Define **vapor pressure** and its significance
- Discuss **cavitation** and its consequences, and do an example problem
- Define **viscosity** and do some example problems that involve viscous forces

Vapor Pressure

$$\left\{ P_v \right\} = \left\{ \frac{F}{L^2} \right\} \quad [P] = [kPa]$$

- The **vapor pressure** P_v of a pure substance is the pressure exerted by its vapor molecules when the system is in phase equilibrium with its liquid molecules at a given temperature (as illustrated in the figure for water).
- **Vapor pressure** (preferred in fluid mechanics) is the same as **saturation pressure** P_{sat} (preferred in thermodynamics).
- When the pressure in a liquid drops below the vapor pressure, the liquid locally vaporizes or “boils” – a process called **cavitation**.
- Cavitation involves the formation of tiny bubbles called **cavitation bubbles**.



Example: Vapor Pressure and Cavitation

Given: Water at 20°C flows at high speed through the narrow gap in a valve. Some calculations indicate that the lowest pressure in the flow is 3220 Pa.

To do: Determine if cavitation is likely to occur in this valve.

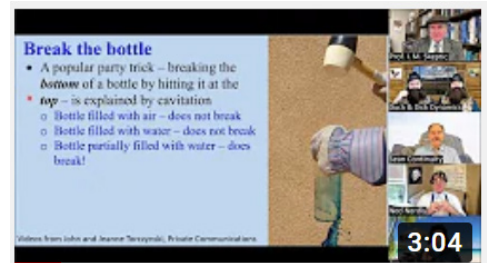
Solution: Look up P_v (or P_{sat}) \rightarrow @ 20°C, $P_v = 2.339 \text{ kPa}$

In our valve, lowest $P = 3220 \text{ Pa} \left(\frac{1 \text{ kPa}}{1000 \text{ Pa}} \right) = \underline{\underline{3.220 \text{ kPa}}}$

* Since $P > P_v$ everywhere, we do not expect cavitation

See my short YouTube video called “**Cool Consequences of Cavitation**” for more about cavitation and some of the interesting problems it causes.

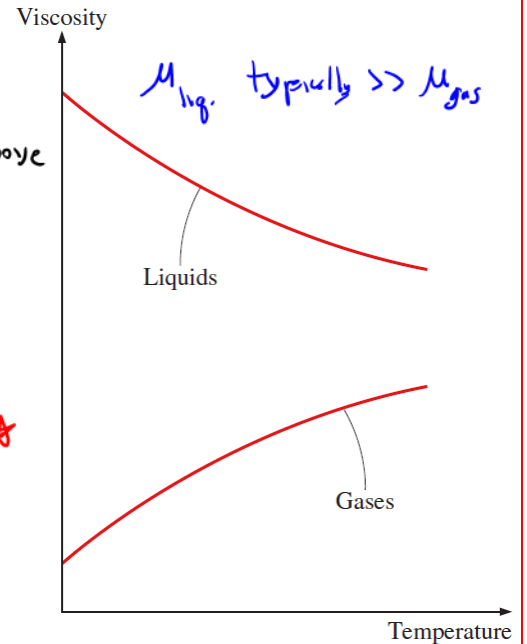
<https://youtu.be/2itqHHCj0dc>



Cool Consequences of Cavitation

Viscosity

- **Viscosity μ** (some authors use η instead) is the fluid property that represents internal resistance of a fluid to motion.
- Viscosity μ is also called **dynamic viscosity**. μ is $\frac{\text{force}}{\text{centipoyce}}$
 $\{\mu\} = \left\{ \frac{\text{m}}{\text{L}\cdot\text{t}} \right\}$ $[\mu] = \left[\frac{\text{kg}}{\text{m}\cdot\text{s}} \right]$ or $[P]$ or $[cP]$
- **Kinematic viscosity ν** is viscosity divided by density, since this combination of variables occurs frequently in fluid mechanics, $\nu = \frac{\mu}{\rho}$. $\{\nu\} = \left\{ \frac{\text{L}^2}{\text{t}} \right\}$, $[\nu] = \left[\frac{\text{m}^2}{\text{s}} \right]$ or $[St]$ Stokes
- The viscosity of gases increases with temperature, while the viscosity of liquids decreases with temperature, as illustrated in the figure.
- For water, μ and/or ν can be found in tables or online.



Some empirical eq's are also available

- For air, μ and/or ν can be found in tables or online. In addition, we use **Sutherland's Law** for calculation of the viscosity of air at a given temperature,

$$\mu \approx \mu_s \left(\frac{T}{T_{s,0}} \right)^{3/2} \frac{T_{s,0} + T_s}{T + T_s}, \quad T_{s,0} = 298.15 \text{ K}, \quad T_s = 110.4 \text{ K}, \quad \mu_s = 1.849 \times 10^{-5} \frac{\text{kg}}{\text{m}\cdot\text{s}}$$

$\mu = \mu(T)$

Example: Viscosity of Air

Given: Air is at 50°C and 1.33 kPa .

ALWAYS USE ABSOLUTE T !!

To do: Calculate the dynamic viscosity and the kinematic viscosity of this air using Sutherland's Law and compare to the values listed in the Appendix at the given temperature.

Solution: $T = (50 + 273.15) \text{ K} = 323.15 \text{ K}$

$$\mu = \left(1.849 \times 10^{-5} \frac{\text{kg}}{\text{m}\cdot\text{s}} \right) \left(\frac{323.15 \text{ K}}{298.15 \text{ K}} \right)^{3/2} \frac{(298.15 + 110.4) \text{ K}}{(323.15 + 110.4) \text{ K}} = 1.9661 \times 10^{-5} \frac{\text{kg}}{\text{m}\cdot\text{s}}$$

$$\mu = 1.97 \times 10^{-5} \frac{\text{kg}}{\text{m}\cdot\text{s}}$$

Appendix table

@ 50°C , $\mu = 1.963 \times 10^{-5} \frac{\text{kg}}{\text{m}\cdot\text{s}}$

error is $\approx 0.2\%$

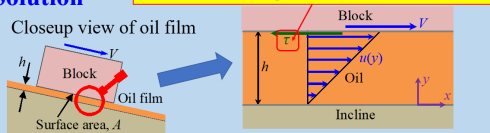
P not used \rightarrow why? $\mu \approx \mu(T)$ only. (μ is a very weak func. of P)

See my short YouTube video called “*Block Sliding Down an Incline on an Oil Film*” for another example that applies viscosity.

<https://youtu.be/8Ai59wQcyOk>

Solution $\tau =$ shear stress acting on bottom surface of the block

• Closeup view of oil film



- The no-slip condition sets
 - $u = 0$ at $y = 0$
 - $u = V$ at $y = h$
- The velocity profile is linear,

$$u(y) = \frac{y}{h} V$$

Solution

• Finally, combine Equations (2) and (3)

$$F_{\text{viscous}} = W \sin \phi = \mu \frac{V}{h} A$$

$$F_{\text{viscous}} = W \sin \phi$$

$$F_{\text{viscous}} = \mu \frac{V}{h} A$$

• Solve for V $V = \frac{W h \sin \phi}{\mu A}$

• This is our final solution for block speed V sliding down the incline

Block Sliding Down an Incline on an Oil Film

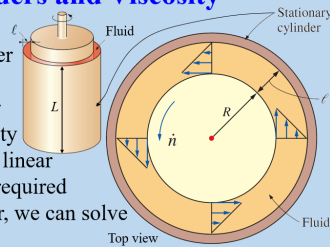
See my short YouTube video called “*TMFM: Fluid Viscosity and Its Bearing on Journal Bearings*” for another example that applies viscosity.

<https://youtu.be/tLvVYGKI2xk>

Co-Rotating Cylinders and Viscosity

- Consider fluid in the thin gap between an inner rotating cylinder and an outer stationary cylinder
- If gap $\ell \ll R$, the velocity profile is approximately linear
- By measuring torque T required to turn the inner cylinder, we can solve for μ ,

$$\mu = \frac{T \ell}{4 \pi^2 R^3 \dot{n} L}$$



Photos from Cengel and Cimbala, *Fluid Mechanics: Fundamentals and Applications*, ed. 4, McGraw-Hill, 2018.

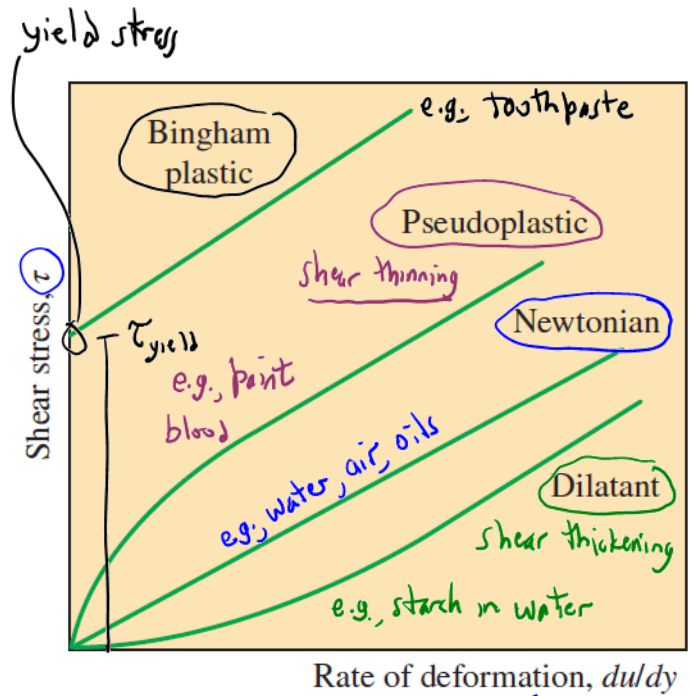
TMFM: Fluid Viscosity and Its Bearing on Journal Bearings

Newtonian vs. Non-Newtonian Fluids

• Newtonian Rate of deformation is linearly proportional to shear stress τ

• For simple shear flows, $\tau = \mu \frac{du}{dy}$ (as in the video examples)

• Non-Newtonian fluids τ ; rate of deformation are not linearly related



WE WILL ANALYZE NEWTONIAN FLUIDS ONLY