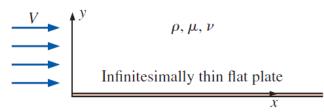
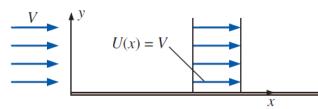
The Laminar Flat Plate Boundary Layer Solution of Blasius (Example 10-10, Çengel and Cimbala)



We go through the steps of the boundary layer procedure:

- Step 1: The outer flow is U(x) = U = V = constant. In other words, the outer flow is simply a uniform stream of constant velocity.
- **Step 2**: A very thin boundary layer is assumed (so thin that it does not affect the outer flow). In other words, the outer flow does not even know that the boundary layer is there.



• Step 3: The boundary layer equations must be solved; they reduce to

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \qquad u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = v \frac{\partial^2 u}{\partial y^2}$$

There are four required boundary conditions,

$$u = 0$$
 at $y = 0$ $u = U$ as $y \to \infty$
 $v = 0$ at $y = 0$ $u = U$ for all y at $x = 0$

as η.

This equation set was first solved by P. R. H. Blasius in 1908 – numerically, but by hand!

Blasius introduced a **similarity variable** η that combines independent variables *x* and *y* into one nondimensional independent variable,

Similarity variable
$$\eta = y \sqrt{\frac{U}{\nu x}}$$
and he solved for a nondimensionalized form of the x-component of
velocity,The similarity
solution is f'
a function of η

The key here is that *one single similarity velocity profile holds for any x-location along the flat plate*. In other words, the velocity profile shape is the same ("similar") at any location, but it is merely *stretched vertically* as the boundary layer grows down the plate. This is illustrated in Fig. 10-98 in the text.

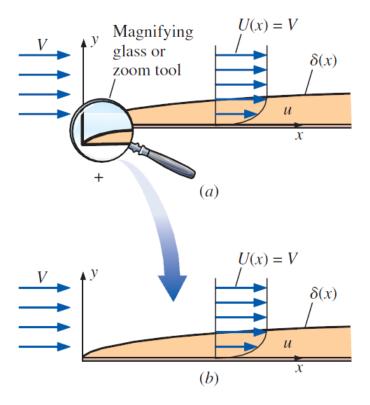
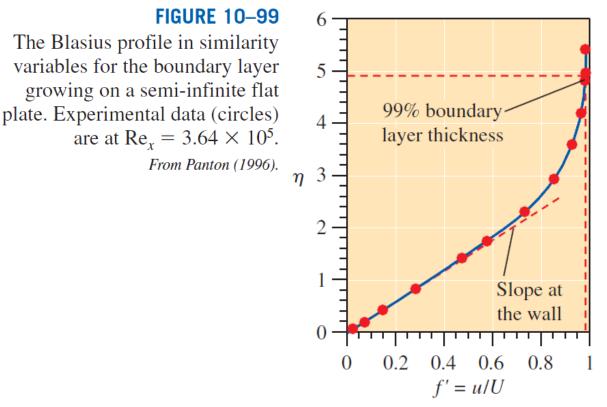


FIGURE 10–98

A useful result of the similarity assumption is that the flow looks the same (is *similar*) regardless of how far we zoom in or out; (*a*) view from a distance, as a person might see, (*b*) close-up view, as an ant might see.

The similarity solution itself is tabulated in Table 10-3, and is plotted in Fig. 10-99.



This one velocity profile, plotted in nondimensional form as above, applies at *any x*- location in the boundary layer.