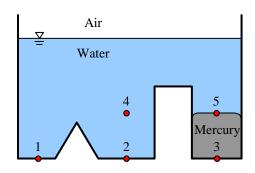
For hydrostatics, pressure can be found from the simple equation, $\frac{P_{\text{below}} = P_{\text{above}} + \rho g \left| \Delta z \right|}{\text{There are several "rules" that directly result from the above equation:}$

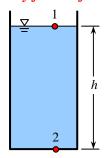
$$P_{\text{below}} = P_{\text{above}} + \rho g \left| \Delta z \right|$$

- 1. If you can draw a continuous line through the same fluid from point 1 to point 2, then $P_1 = P_2$ if $z_1 = z_2$.

E.g., consider the oddly shaped container in the sketch. By this rule, $P_1 = P_2$ and $P_4 = P_5$ since these points are at the same elevation in the same fluid. However, P_2 does not equal P_3 even though they are at the same elevation, because one cannot draw a line connecting these points through the same fluid. In fact, P_2 is less than P_3 since mercury is denser than water.



2. Any free surface open to the atmosphere has atmospheric pressure, P_{atm}

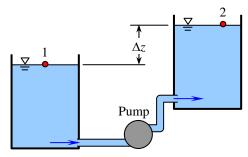


(This rule holds not only for hydrostatics, by the way, but for any free surface exposed to the atmosphere, whether that surface is moving, stationary, flat, or curved.) Consider the hydrostatics example of a container of water. The little upside-down triangle indicates a free surface, and means that the pressure there is atmospheric pressure, P_{atm} . In other words, in this example, $P_1 = P_{\text{atm}}$. To find the pressure at point 2, our hydrostatics equation is used:

$$P_{\text{below}} = P_{\text{above}} + \rho g |\Delta z|$$

 $P_2 = P_1 + \rho g h$
 $P_2 = P_{\text{atm}} + \rho g h$ (absolute pressure)
Or, $P_{2,\text{gage}} = \rho g h$ (gage pressure)

3. In most practical problems, atmospheric pressure is assumed to be constant at all elevations (unless the change in elevation is large). Consider the example shown, in which water is pumped from one large reservoir to another. The pressure at both 1 and 2 is atmospheric. But since point 2 is higher in elevation than point 1, the local atmospheric pressure at 2 is a little lower than that at point 1. To be precise, our hydrostatics equation may be used to account for the difference in elevation between points 1 and 2. However, since the density of water is so much greater than that of air, it is common to ignore the difference between P_1 and P_2 , and call them both the same value of atmospheric pressure, P_{atm} .

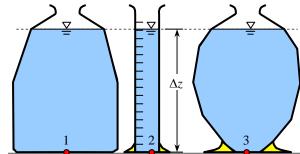


4. The shape of a container does not matter in hydrostatics. (Except of course for very small diameter tubes, where

surface tension and the capillary effect become important.) Consider the three containers in the figure. At first glance, it may seem that the pressure at point 3 would be greater than that at point 2, since the weight of the water is more "concentrated" on the small area at the bottom, but in reality, all three pressures are identical. Use of our hydrostatics equation confirms this conclusion, i.e.,

$$P_{\text{below}} = P_{\text{above}} + \rho g \left| \Delta z \right|$$

$$P_{1} = P_{2} = P_{3} = P_{\text{atm}} + \rho g \Delta z$$



In all three cases, a thin column of water above the point in question at the bottom is identical. Pressure is a force per unit area, and over a small area at the bottom, that force is due to the weight of the water above it, which is the same in all three cases, regardless of the container shape.

5. Pressure is constant across a flat fluid-fluid interface.

For example, consider the container in the figure, which is partially filled with mercury, and partially with water. In this case, our hydrostatics equation must be used twice, once in each of the liquids.

$$\begin{split} P_{\text{below}} &= P_{\text{above}} + \rho g \left| \Delta z \right| \\ P_{1} &= P_{\text{atm}} + \rho_{\text{water}} g \Delta z_{1} \\ P_{2} &= P_{1} + \rho_{\text{mercury}} g \Delta z_{2} = P_{\text{atm}} + \rho_{\text{water}} g \Delta z_{1} + \rho_{\text{mercury}} g \Delta z_{2} \end{split}$$

Note that if the interface is not flat, but curved, there will be a pressure difference across that interface.

