Area A(z) under the normal PDF, f(z)

| $A(z) = \frac{1}{2} \operatorname{erf}\left(\frac{z}{\sqrt{2}}\right)$ | where | $z = \frac{x - \mu}{\sigma} \approx$ | $\frac{x-\overline{x}}{S}$ |
|--|-----------|--------------------------------------|----------------------------|
| Example, at $z = 1.0$ | 6, A(z) = | = 0.35543. | |



| Z | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 0.0 | 0.00000 | 0.00399 | 0.00798 | 0.01197 | 0.01595 | 0.01994 | 0.02392 | 0.02790 | 0.03188 | 0.03586 |
| 0.1 | 0.03983 | 0.04380 | 0.04776 | 0.05172 | 0.05567 | 0.05962 | 0.06356 | 0.06749 | 0.07142 | 0.07535 |
| 0.2 | 0.07926 | 0.08317 | 0.08706 | 0.09095 | 0.09483 | 0.09871 | 0.10257 | 0.10642 | 0.11026 | 0.11409 |
| 0.3 | 0.11791 | 0.12172 | 0.12552 | 0.12930 | 0.13307 | 0.13683 | 0.14058 | 0.14431 | 0.14803 | 0.15173 |
| 0.4 | 0.15542 | 0.15910 | 0.16276 | 0.16640 | 0.17003 | 0.17364 | 0.17724 | 0.18082 | 0.18439 | 0.18793 |
| 0.5 | 0.19146 | 0.19497 | 0.19847 | 0.20194 | 0.20540 | 0.20884 | 0.21226 | 0.21566 | 0.21904 | 0.22240 |
| 0.6 | 0.22575 | 0.22907 | 0.23237 | 0.23565 | 0.23891 | 0.24215 | 0.24537 | 0.24857 | 0.25175 | 0.25490 |
| 0.7 | 0.25804 | 0.26115 | 0.26424 | 0.26730 | 0.27035 | 0.27337 | 0.27637 | 0.27935 | 0.28230 | 0.28524 |
| 0.8 | 0.28814 | 0.29103 | 0.29389 | 0.29673 | 0.29955 | 0.30234 | 0.30511 | 0.30785 | 0.31057 | 0.31327 |
| 0.9 | 0.31594 | 0.31859 | 0.32121 | 0.32381 | 0.32639 | 0.32894 | 0.33147 | 0.33398 | 0.33646 | 0.33891 |
| 1.0 | 0.34134 | 0.34375 | 0.34614 | 0.34849 | 0.35083 | 0.35314 | 0.35543 | 0.35769 | 0.35993 | 0.36214 |
| 1.1 | 0.36433 | 0.36650 | 0.36864 | 0.37076 | 0.37286 | 0.37493 | 0.37698 | 0.37900 | 0.38100 | 0.38298 |
| 1.2 | 0.38493 | 0.38686 | 0.38877 | 0.39065 | 0.39251 | 0.39435 | 0.39617 | 0.39796 | 0.39973 | 0.40147 |
| 1.3 | 0.40320 | 0.40490 | 0.40658 | 0.40824 | 0.40988 | 0.41149 | 0.41309 | 0.41466 | 0.41621 | 0.41774 |
| 1.4 | 0.41924 | 0.42073 | 0.42220 | 0.42364 | 0.42507 | 0.42647 | 0.42785 | 0.42922 | 0.43056 | 0.43189 |
| 1.5 | 0.43319 | 0.43448 | 0.43574 | 0.43699 | 0.43822 | 0.43943 | 0.44062 | 0.44179 | 0.44295 | 0.44408 |
| 1.6 | 0.44520 | 0.44630 | 0.44738 | 0.44845 | 0.44950 | 0.45053 | 0.45154 | 0.45254 | 0.45352 | 0.45449 |
| 1.7 | 0.45543 | 0.45637 | 0.45728 | 0.45818 | 0.45907 | 0.45994 | 0.46080 | 0.46164 | 0.46246 | 0.46327 |
| 1.8 | 0.46407 | 0.46485 | 0.46562 | 0.46638 | 0.46712 | 0.46784 | 0.46856 | 0.46926 | 0.46995 | 0.47062 |
| 1.9 | 0.47128 | 0.47193 | 0.47257 | 0.47320 | 0.47381 | 0.47441 | 0.47500 | 0.47558 | 0.47615 | 0.47670 |
| 2.0 | 0.47725 | 0.47778 | 0.47831 | 0.47882 | 0.47932 | 0.47982 | 0.48030 | 0.48077 | 0.48124 | 0.48169 |
| 2.1 | 0.48214 | 0.48257 | 0.48300 | 0.48341 | 0.48382 | 0.48422 | 0.48461 | 0.48500 | 0.48537 | 0.48574 |
| 2.2 | 0.48610 | 0.48645 | 0.48679 | 0.48713 | 0.48745 | 0.48778 | 0.48809 | 0.48840 | 0.48870 | 0.48899 |
| 2.3 | 0.48928 | 0.48956 | 0.48983 | 0.49010 | 0.49036 | 0.49061 | 0.49086 | 0.49111 | 0.49134 | 0.49158 |
| 2.4 | 0.49180 | 0.49202 | 0.49224 | 0.49245 | 0.49266 | 0.49286 | 0.49305 | 0.49324 | 0.49343 | 0.49361 |
| 2.5 | 0.49379 | 0.49396 | 0.49413 | 0.49430 | 0.49446 | 0.49461 | 0.49477 | 0.49492 | 0.49506 | 0.49520 |
| 2.6 | 0.49534 | 0.49547 | 0.49560 | 0.49573 | 0.49585 | 0.49598 | 0.49609 | 0.49621 | 0.49632 | 0.49643 |
| 2.7 | 0.49653 | 0.49664 | 0.49674 | 0.49683 | 0.49693 | 0.49702 | 0.49711 | 0.49720 | 0.49728 | 0.49736 |
| 2.8 | 0.49744 | 0.49752 | 0.49760 | 0.49767 | 0.49774 | 0.49781 | 0.49788 | 0.49795 | 0.49801 | 0.49807 |
| 2.9 | 0.49813 | 0.49819 | 0.49825 | 0.49831 | 0.49836 | 0.49841 | 0.49846 | 0.49851 | 0.49856 | 0.49861 |
| 3.0 | 0.49865 | 0.49869 | 0.49874 | 0.49878 | 0.49882 | 0.49886 | 0.49889 | 0.49893 | 0.49896 | 0.49900 |
| 3.1 | 0.49903 | 0.49906 | 0.49910 | 0.49913 | 0.49916 | 0.49918 | 0.49921 | 0.49924 | 0.49926 | 0.49929 |
| 3.2 | 0.49931 | 0.49934 | 0.49936 | 0.49938 | 0.49940 | 0.49942 | 0.49944 | 0.49946 | 0.49948 | 0.49950 |
| 3.3 | 0.49952 | 0.49953 | 0.49955 | 0.49957 | 0.49958 | 0.49960 | 0.49961 | 0.49962 | 0.49964 | 0.49965 |
| 3.4 | 0.49966 | 0.49968 | 0.49969 | 0.49970 | 0.49971 | 0.49972 | 0.49973 | 0.49974 | 0.49975 | 0.49976 |
| 3.5 | 0.49977 | 0.49978 | 0.49978 | 0.49979 | 0.49980 | 0.49981 | 0.49981 | 0.49982 | 0.49983 | 0.49983 |
| 3.6 | 0.49984 | 0.49985 | 0.49985 | 0.49986 | 0.49986 | 0.49987 | 0.49987 | 0.49988 | 0.49988 | 0.49989 |
| 3.7 | 0.49989 | 0.49990 | 0.49990 | 0.49990 | 0.49991 | 0.49991 | 0.49992 | 0.49992 | 0.49992 | 0.49992 |
| 3.8 | 0.49993 | 0.49993 | 0.49993 | 0.49994 | 0.49994 | 0.49994 | 0.49994 | 0.49995 | 0.49995 | 0.49995 |
| 3.9 | 0.49995 | 0.49995 | 0.49996 | 0.49996 | 0.49996 | 0.49996 | 0.49996 | 0.49996 | 0.49997 | 0.49997 |
| 4.0 | 0.49997 | 0.49997 | 0.49997 | 0.49997 | 0.49997 | 0.49997 | 0.49998 | 0.49998 | 0.49998 | 0.49998 |

| Values | Values of $t_{\alpha/2}$ (critical values) for the student's t distribution | | | | | | | | | | | |
|------------------------|---|----------------|----------------|----------------|--|--|--|--|--|--|--|--|
| | 90% confidence | 95% confidence | 98% confidence | 99% confidence | | | | | | | | |
| $\alpha = \rightarrow$ | 0.10 | 0.05 | 0.02 | 0.01 | | | | | | | | |
| df = ↓ | | | | | | | | | | | | |
| 1 | 6.3137 | 12.7062 | 31.8210 | 63.6559 | | | | | | | | |
| 2 | 2.9200 | 4.3027 | 6.9645 | 9.9250 | | | | | | | | |
| 3 | 2.3534 | 3.1824 | 4.5407 | 5.8408 | | | | | | | | |
| 4 | 2.1318 | 2.7765 | 3.7469 | 4.6041 | | | | | | | | |
| 5 | 2.0150 | 2.5706 | 3.3649 | 4.0321 | | | | | | | | |
| 6 | 1.9432 | 2.4469 | 3.1427 | 3.7074 | | | | | | | | |
| 7 | 1.8946 | 2.3646 | 2.9979 | 3.4995 | | | | | | | | |
| 8 | 1.8595 | 2.3060 | 2.8965 | 3.3554 | | | | | | | | |
| 9 | 1.8331 | 2.2622 | 2.8214 | 3.2498 | | | | | | | | |
| 10 | 1.8125 | 2.2281 | 2.7638 | 3.1693 | | | | | | | | |
| 11 | 1.7959 | 2.2010 | 2.7181 | 3.1058 | | | | | | | | |
| 12 | 1.7823 | 2.1788 | 2.6810 | 3.0545 | | | | | | | | |
| 13 | 1.7709 | 2.1604 | 2.6503 | 3.0123 | | | | | | | | |
| 14 | 1.7613 | 2.1448 | 2.6245 | 2.9768 | | | | | | | | |
| 15 | 1.7531 | 2.1315 | 2.6025 | 2.9467 | | | | | | | | |
| 16 | 1.7459 | 2.1199 | 2.5835 | 2.9208 | | | | | | | | |
| 17 | 1.7396 | 2.1098 | 2.5669 | 2.8982 | | | | | | | | |
| 18 | 1.7341 | 2.1009 | 2.5524 | 2.8784 | | | | | | | | |
| 19 | 1.7291 | 2.0930 | 2.5395 | 2.8609 | | | | | | | | |
| 20 | 1.7247 | 2.0860 | 2.5280 | 2.8453 | | | | | | | | |
| 21 | 1.7207 | 2.0796 | 2.5176 | 2.8314 | | | | | | | | |
| 22 | 1.7171 | 2.0739 | 2.5083 | 2.8188 | | | | | | | | |
| 23 | 1.7139 | 2.0687 | 2.4999 | 2.8073 | | | | | | | | |
| 24 | 1.7109 | 2.0639 | 2.4922 | 2.7970 | | | | | | | | |
| 25 | 1.7081 | 2.0595 | 2.4851 | 2.7874 | | | | | | | | |
| 26 | 1.7056 | 2.0555 | 2.4786 | 2.7787 | | | | | | | | |
| 27 | 1.7033 | 2.0518 | 2.4727 | 2.7707 | | | | | | | | |
| 28 | 1.7011 | 2.0484 | 2.4671 | 2.7633 | | | | | | | | |
| 29 | 1.6991 | 2.0452 | 2.4620 | 2.7564 | | | | | | | | |
| 30 | 1.6973 | 2.0423 | 2.4573 | 2.7500 | | | | | | | | |
| 35 | 1.6896 | 2.0301 | 2.4377 | 2.7238 | | | | | | | | |
| 40 | 1.6839 | 2.0211 | 2.4233 | 2.7045 | | | | | | | | |
| 50 | 1.6759 | 2.0086 | 2.4033 | 2.6778 | | | | | | | | |
| 100 | 1.6602 | 1.9840 | 2.3642 | 2.6259 | | | | | | | | |
| 500 | 1.6479 | 1.9647 | 2.3338 | 2.5857 | | | | | | | | |
| 1000 | 1.6464 | 1.9623 | 2.3301 | 2.5807 | | | | | | | | |
| 1.00E+10 | 1.6448 | 1.9600 | 2.3264 | 2.5758 | | | | | | | | |

Critical Values for the Student's *t* Distribution

| Critical | Values | for the | χ^2 | PDF |
|----------|--------|---------|----------|-----|
|----------|--------|---------|----------|-----|

| Criti | Critical values of $\chi^2_{1-\alpha/2}$ and $\chi^2_{\alpha/2}$ for the χ^2 distribution (both tails) | | | | | | | | | | | |
|---------------------------|---|--------------------|-----------------------|---------------------|----------------------|----------------------------|-----------------------|----------------------------|--|--|--|--|
| Two tails \rightarrow | 90% co | nfidence | 95% co | nfidence | 98% co | nfidence | 99% confidence | | | | | |
| $\alpha \rightarrow$ | 0. | 10 | 0. | 05 | 0. | 02 | 0. | 01 | | | | |
| Single tail \rightarrow | $1-\alpha/2$ | α/2 | $1-\alpha/2$ | α/2 | $1-\alpha/2$ | α/2 | $1-\alpha/2$ | α/2 | | | | |
| Probability \rightarrow | 0.95 | 0.05 | 0.975 | 0.025 | 0.99 | 0.01 | 0.995 | 0.005 | | | | |
| df = ↓ | X ² 1-a./2 | χ ² α/2 | X ² 1-a./2 | X ² a./2 | X ² 1-æ/2 | X ² a./2 | X ² 1-a./2 | X ² a./2 | | | | |
| 1 | 0.0039 | 3.8415 | 0.0010 | 5.0239 | 0.0002 | 6.6349 | 0.0000 | 7.8794 | | | | |
| 2 | 0.1026 | 5.9915 | 0.0506 | 7.3778 | 0.0201 | 9.2104 | 0.0100 | 10.5965 | | | | |
| 3 | 0.3518 | 7.8147 | 0.2158 | 9.3484 | 0.1148 | 11.3449 | 0.0717 | 12.8381 | | | | |
| 4 | 0.7107 | 9.4877 | 0.4844 | 11.1433 | 0.2971 | 13.2767 | 0.2070 | 14.8602 | | | | |
| 5 | 1.1455 | 11.0705 | 0.8312 | 12.8325 | 0.5543 | 15.0863 | 0.4118 | 16.7496 | | | | |
| 6 | 1.6354 | 12.5916 | 1.2373 | 14.4494 | 0.8721 | 16.8119 | 0.6757 | 18.5475 | | | | |
| 7 | 2.1673 | 14.0671 | 1.6899 | 16.0128 | 1.2390 | 18.4753 | 0.9893 | 20.2777 | | | | |
| 8 | 2.7326 | 15.5073 | 2.1797 | 17.5345 | 1.6465 | 20.0902 | 1.3444 | 21.9549 | | | | |
| 9 | 3.3251 | 16.9190 | 2.7004 | 19.0228 | 2.0879 | 21.6660 | 1.7349 | 23.5893 | | | | |
| 10 | 3.9403 | 18.3070 | 3.2470 | 20.4832 | 2.5582 | 23.2093 | 2.1558 | 25.1881 | | | | |
| 11 | 4.5748 | 19.6752 | 3.8157 | 21.9200 | 3.0535 | 24.7250 | 2.6032 | 26.7569 | | | | |
| 12 | 5.2260 | 21.0261 | 4.4038 | 23.3367 | 3.5706 | 26.2170 | 3.0738 | 28.2997 | | | | |
| 13 | 5.8919 | 22.3620 | 5.0087 | 24.7356 | 4.1069 | 27.6882 | 3.5650 | 29.8193 | | | | |
| 14 | 6.5706 | 23.6848 | 5.6287 | 26.1189 | 4.6604 | 29.1412 | 4.0747 | 31.3194 | | | | |
| 15 | 7.2609 | 24.9958 | 6.2621 | 27.4884 | 5.2294 | 30.5780 | 4.6009 | 32.8015 | | | | |
| 16 | 7.9616 | 26.2962 | 6.9077 | 28.8453 | 5.8122 | 31.9999 | 5.1422 | 34.2671 | | | | |
| 17 | 8.6718 | 27.5871 | 7.5642 | 30.1910 | 6.4077 | 33.4087 | 5.6973 | 35.7184 | | | | |
| 18 | 9.3904 | 28.8693 | 8.2307 | 31.5264 | 7.0149 | 34.8052 | 6.2648 | 37.1564 | | | | |
| 19 | 10.1170 | 30.1435 | 8.9065 | 32.8523 | 7.6327 | 36.1908 | 6.8439 | 38.5821 | | | | |
| 20 | 10.8508 | 31.4104 | 9.5908 | 34.1696 | 8.2604 | 37.5663 | 7.4338 | 39.9969 | | | | |
| 21 | 11.5913 | 32.6706 | 10.2829 | 35.4789 | 8.8972 | 38.9322 | 8.0336 | 41.4009 | | | | |
| 22 | 12.3380 | 33.9245 | 10.9823 | 36.7807 | 9.5425 | 40.2894 | 8.6427 | 42.7957 | | | | |
| 23 | 13.0905 | 35.1725 | 11.6885 | 38.0756 | 10.1957 | 41.6383 | 9.2604 | 44.1814 | | | | |
| 24 | 13.8484 | 36.4150 | 12.4011 | 39.3641 | 10.8563 | 42.9798 | 9.8862 | 45.5584 | | | | |
| 25 | 14.6114 | 37.6525 | 13.1197 | 40.6465 | 11.5240 | 44.3140 | 10.5196 | 46.9280 | | | | |
| 26 | 15.3792 | 38.8851 | 13.8439 | 41.9231 | 12.1982 | 45.6416 | 11.1602 | 48.2898 | | | | |
| 27 | 16.1514 | 40.1133 | 14.5734 | 43.1945 | 12.8785 | 46.9628 | 11.8077 | 49.6450 | | | | |
| 28 | 16.9279 | 41.3372 | 15.3079 | 44.4608 | 13.5647 | 48.2782 | 12.4613 | 50.9936 | | | | |
| 29 | 17.7084 | 42.5569 | 16.0471 | 45.7223 | 14.2564 | 49.5878 | 13.1211 | 52.3355 | | | | |
| 30 | 18.4927 | 43.7730 | 16.7908 | 46.9792 | 14.9535 | 50.8922 | 13.7867 | 53.6719 | | | | |
| 35 | 22.4650 | 49.8018 | 20.5694 | 53.2033 | 18.5089 | 57.3420 | 17.1917 | 60.2746 | | | | |
| 40 | 26.5093 | 55.7585 | 24.4331 | 59.3417 | 22.1642 | 63.6908 | 20.7066 | 66.7660 | | | | |
| 50 | 34.7642 | 67.5048 | 32.3574 | 71.4202 | 29.7067 | 76.1538 | 27.9908 | 79.4898 | | | | |
| 100 | 77.9294 | 124.3421 | 74.2219 | 129.5613 | 70.0650 | 135.8069 | 67.3275 | 140.1697 | | | | |
| 500 | 449.1467 | 553.1269 | 439.9360 | 563.8514 | 429.3874 | 576.4931 | 422.3034 | 585.2060 | | | | |
| 1000 | 927.5944 | 1074.6794 | 914.2572 | 1089.5307 | 898.9124 | 1106.9690 | 888.5631 | 1118.9475 | | | | |
| 00 | œ | 8 | 8 | 8 | 8 | œ | 8 | 8 | | | | |

Critical Values of the Linear Correlation Coefficient

| Values | Values of r_t (critical values) for linear correlation coefficient | | | | | | | | | | | |
|------------------------|--|---------|----------|---------|---------|----------|---------|---------|--|--|--|--|
| $c = \rightarrow$ | 80% | 90% | 92.5% | 95% | 97% | 98% | 99% | 99.5% | | | | |
| $\alpha = \rightarrow$ | 0.2 | 0.1 | 0.075 | 0.05 | 0.03 | 0.02 | 0.01 | 0.005 | | | | |
| $n = \downarrow$ | | | | | | | | | | | | |
| 3 | 0.95106 | 0.98769 | 0.99307 | 0.99692 | 0.99889 | 0.99951 | 0.99988 | 0.99997 | | | | |
| 4 | 0.80000 | 0.90000 | 0.92500 | 0.95000 | 0.97000 | 0.98000 | 0.99000 | 0.99500 | | | | |
| 5 | 0.68705 | 0.80538 | 0.83994 | 0.87834 | 0.91377 | 0.93433 | 0.95874 | 0.97404 | | | | |
| 6 | 0.60840 | 0.72930 | 0.76718 | 0.81140 | 0.85503 | 0.88219 | 0.91720 | 0.94170 | | | | |
| 7 | 0.55086 | 0.66944 | 0.70809 | 0.75449 | 0.80206 | 0.83287 | 0.87453 | 0.90556 | | | | |
| 8 | 0.50673 | 0.62149 | 0.65985 | 0.70673 | 0.75599 | 0.78872 | 0.83434 | 0.86974 | | | | |
| 9 | 0.47159 | 0.58221 | 0.61982 | 0.66638 | 0.71613 | 0.74978 | 0.79768 | 0.83591 | | | | |
| 10 | 0.44280 | 0.54936 | 0.58606 | 0.63190 | 0.68148 | 0.71546 | 0.76459 | 0.80461 | | | | |
| 11 | 0.41866 | 0.52140 | 0.55713 | 0.60207 | 0.65114 | 0.68510 | 0.73479 | 0.77589 | | | | |
| 12 | 0.39806 | 0.49726 | 0.53202 | 0.57598 | 0.62434 | 0.65807 | 0.70789 | 0.74961 | | | | |
| 13 | 0.38022 | 0.47616 | 0.50998 | 0.55294 | 0.60049 | 0.63386 | 0.68353 | 0.72553 | | | | |
| 14 | 0.36456 | 0.45750 | 0.49043 | 0.53241 | 0.57911 | 0.61205 | 0.66138 | 0.70344 | | | | |
| 15 | 0.35069 | 0.44086 | 0.47295 | 0.51398 | 0.55980 | 0.59227 | 0.64114 | 0.68311 | | | | |
| 16 | 0.33828 | 0.42590 | 0.45719 | 0.49731 | 0.54227 | 0.57425 | 0.62259 | 0.66434 | | | | |
| 17 | 0.32710 | 0.41236 | 0.44290 | 0.48215 | 0.52627 | 0.55774 | 0.60551 | 0.64696 | | | | |
| 18 | 0.31696 | 0.40003 | 0.42986 | 0.46828 | 0.51158 | 0.54255 | 0.58971 | 0.63083 | | | | |
| 19 | 0.30770 | 0.38873 | 0.41791 | 0.45553 | 0.49804 | 0.52852 | 0.57507 | 0.61580 | | | | |
| 20 | 0.29921 | 0.37834 | 0.40689 | 0.44376 | 0.48551 | 0.51550 | 0.56144 | 0.60176 | | | | |
| 22 | 0.28414 | 0.35983 | 0.38723 | 0.42271 | 0.46303 | 0.49209 | 0.53680 | 0.57627 | | | | |
| 24 | 0.27114 | 0.34378 | 0.37016 | 0.40439 | 0.44338 | 0.47158 | 0.51510 | 0.55370 | | | | |
| 26 | 0.25977 | 0.32970 | 0.35516 | 0.38824 | 0.42603 | 0.45341 | 0.49581 | 0.53355 | | | | |
| 28 | 0.24972 | 0.31722 | 0.34184 | 0.37389 | 0.41055 | 0.43718 | 0.47851 | 0.51542 | | | | |
| 30 | 0.24075 | 0.30606 | 0.32991 | 0.36101 | 0.39664 | 0.42257 | 0.46289 | 0.49900 | | | | |
| 32 | 0.23268 | 0.29599 | 0.31915 | 0.34937 | 0.38405 | 0.40933 | 0.44870 | 0.48404 | | | | |
| 34 | 0.22537 | 0.28686 | 0.30938 | 0.33879 | 0.37259 | 0.39725 | 0.43573 | 0.47034 | | | | |
| 36 | 0.21871 | 0.27852 | 0.30045 | 0.32911 | 0.36209 | 0.38618 | 0.42381 | 0.45773 | | | | |
| 38 | 0.21261 | 0.27086 | 0.29225 | 0.32022 | 0.35243 | 0.37598 | 0.41282 | 0.44608 | | | | |
| 40 | 0.20699 | 0.26381 | 0.28469 | 0.31201 | 0.34350 | 0.36655 | 0.40264 | 0.43527 | | | | |
| 45 | 0.19469 | 0.24833 | 0.26808 | 0.29396 | 0.32384 | 0.34575 | 0.38014 | 0.41133 | | | | |
| 50 | 0.18434 | 0.23529 | 0.25407 | 0.27871 | 0.30720 | 0.32813 | 0.36103 | 0.39093 | | | | |
| 55 | 0.17549 | 0.22411 | 0.24205 | 0.26561 | 0.29289 | 0.31295 | 0.34453 | 0.37329 | | | | |
| 60 | 0.16780 | 0.21438 | 0.23159 | 0.25420 | 0.28041 | 0.29970 | 0.33010 | 0.35783 | | | | |
| 05 | 0.16104 | 0.20582 | 0.22238 | 0.24415 | 0.26940 | 0.28799 | 0.31735 | 0.34414 | | | | |
| /0 | 0.15504 | 0.19821 | 0.21419 | 0.23520 | 0.25959 | 0.27756 | 0.30596 | 0.33191 | | | | |
| 80 | 0.14480 | 0.18522 | 0.20019 | 0.21990 | 0.24280 | 0.25970 | 0.28043 | 0.31091 | | | | |
| 90 | 0.13030 | 0.1/449 | 0.10003 | 0.20725 | 0.22890 | 0.24490 | 0.27022 | 0.29345 | | | | |
| 100 | 0.12924 | 0.10343 | 0.1/600 | 0.19035 | 0.21/14 | 0.23230 | 0.20048 | 0.27803 | | | | |
| 200 | 0.10323 | 0.13462 | 0.14362 | 0.10055 | 0.17/20 | 0.16900 | 0.20973 | 0.10776 | | | | |
| 200 | 0.09100 | 0.00515 | 0.102019 | 0.13879 | 0.13530 | 0.10441 | 0.101/0 | 0.19770 | | | | |
| 400 | 0.06421 | 0.09313 | 0.08012 | 0.00807 | 0.12352 | 0.11620 | 0.14051 | 0.14010 | | | | |
| 500 | 0.05741 | 0.07364 | 0.07970 | 0.08770 | 0.09706 | 0 10402 | 0.11510 | 0 12535 | | | | |
| 1000 | 0.04056 | 0.05204 | 0.05633 | 0.06200 | 0.06863 | 0.07356 | 0.08142 | 0.08870 | | | | |
| 1000 | 0.01000 | 0.00201 | 0.00000 | 0.00200 | 0.00000 | 0.070000 | 0.001.2 | 0.00070 | | | | |

Modified Thompson Tau – Used for Determination of Outliers

In this table, τ is obtained from the expression

$$\tau = \frac{t \cdot (n-1)}{\sqrt{n}\sqrt{n-2+t^2}}, \text{ where }$$

- *n* is the number of data points
- *t* is the student's *t* value, based on $\alpha = 0.05$ and df = *n*-2 (note that here df = *n*-2 instead of *n*-1). In Excel, we calculate *t* as TINV(α , df), i.e., here *t* = TINV(α , *n*-2)

| Values | s of the M | odified Tl | nom | pson $	au$ |
|--------|------------|------------|-------------|------------|
| n | τ | | n | τ |
| 3 | 1.1511 | | 33 | 1.9160 |
| 4 | 1.4250 | | 34 | 1.9174 |
| 5 | 1.5712 | | 35 | 1.9186 |
| 6 | 1.6563 | | 36 | 1.9198 |
| 7 | 1.7110 | | 37 | 1.9209 |
| 8 | 1.7491 | | 38 | 1.9220 |
| 9 | 1.7770 | | 39 | 1.9230 |
| 10 | 1.7984 | | 40 | 1.9240 |
| 11 | 1.8153 | | 42 | 1.9257 |
| 12 | 1.8290 | | 44 | 1.9273 |
| 13 | 1.8403 | | 46 | 1.9288 |
| 14 | 1.8498 | | 48 | 1.9301 |
| 15 | 1.8579 | | 50 | 1.9314 |
| 16 | 1.8649 | | 52 | 1.9325 |
| 17 | 1.8710 | | 54 | 1.9335 |
| 18 | 1.8764 | | 56 | 1.9345 |
| 19 | 1.8811 | | 58 | 1.9354 |
| 20 | 1.8853 | | 60 | 1.9362 |
| 21 | 1.8891 | | 65 | 1.9381 |
| 22 | 1.8926 | | 70 | 1.9397 |
| 23 | 1.8957 | | 75 | 1.9411 |
| 24 | 1.8985 | | 80 | 1.9423 |
| 25 | 1.9011 | | 90 | 1.9443 |
| 26 | 1.9035 | 1 | 100 | 1.9459 |
| 27 | 1.9057 | 1 | 150 | 1.9506 |
| 28 | 1.9078 | 2 | 200 | 1.9530 |
| 29 | 1.9096 | 4 | 500 | 1.9572 |
| 30 | 1.9114 | 10 | 000 | 1.9586 |
| 31 | 1.9130 | 50 | 000 | 1.9597 |
| 32 | 1.9146 | (→ | (00) | 1.9600 |

p-Values for the *t* Distribution – <u>one tail</u>, df = 9

For *two tails*, multiply the value by 2, since the *t* PDF is symmetric. The *p*-value is the colored area under the *t* PDF in the sketch.



Example: 1-tailed p at t = 1.06: p-value = TDIST(t,df,1) = 0.15838. 2-tailed p at t = 1.06: p-value = TDIST(t,df,2) = 0.31676.

| t | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
|-----|----------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 0.0 | 0.50000 | 0.49612 | 0.49224 | 0.48836 | 0.48448 | 0.48061 | 0.47673 | 0.47286 | 0.46899 | 0.46513 |
| 0.1 | 0.46127 | 0.45741 | 0.45356 | 0.44971 | 0.44587 | 0.44204 | 0.43821 | 0.43439 | 0.43057 | 0.42676 |
| 0.2 | 0.42296 | 0.41917 | 0.41539 | 0.41162 | 0.40785 | 0.40410 | 0.40036 | 0.39662 | 0.39290 | 0.38919 |
| 0.3 | 0.38550 | 0.38181 | 0.37814 | 0.37448 | 0.37083 | 0.36719 | 0.36358 | 0.35997 | 0.35638 | 0.35280 |
| 0.4 | 0.34924 | 0.34570 | 0.34217 | 0.33865 | 0.33516 | 0.33168 | 0.32821 | 0.32477 | 0.32134 | 0.31793 |
| 0.5 | 0.31454 | 0.31116 | 0.30781 | 0.30447 | 0.30115 | 0.29785 | 0.29457 | 0.29131 | 0.28807 | 0.28485 |
| 0.6 | 0.28165 | 0.27847 | 0.27532 | 0.27218 | 0.26906 | 0.26597 | 0.26289 | 0.25984 | 0.25681 | 0.25380 |
| 0.7 | 0.25081 | 0.24784 | 0.24490 | 0.24198 | 0.23908 | 0.23620 | 0.23335 | 0.23052 | 0.22771 | 0.22492 |
| 0.8 | 0.22216 | 0.21942 | 0.21670 | 0.21400 | 0.21133 | 0.20868 | 0.20606 | 0.20345 | 0.20087 | 0.19832 |
| 0.9 | 0.19578 | 0.19327 | 0.19079 | 0.18832 | 0.18588 | 0.18346 | 0.18107 | 0.17870 | 0.17635 | 0.17402 |
| 1.0 | 0.1/1/2 | 0.16944 | 0.16/18 | 0.16495 | 0.162/4 | 0.16055 | 0.15838 | 0.15624 | 0.15412 | 0.15202 |
| 1.1 | 0.14994 | 0.14/89 | 0.14580 | 0.14385 | 0.14180 | 0.13989 | 0.13/95 | 0.13003 | 0.13412 | 0.13224 |
| 1.2 | 0.13039 | 0.12855 | 0.120/3 | 0.12494 | 0.12517 | 0.12141 | 0.11908 | 0.11/9/ | 0.11028 | 0.00907 |
| 1.5 | 0.00751 | 0.00607 | 0.109/1 | 0.00325 | 0.10035 | 0.10499 | 0.10340 | 0.10194 | 0.10045 | 0.09697 |
| 1.4 | 0.09751 | 0.03007 | 0.03403 | 0.09323 | 0.07897 | 0.07778 | 0.03915 | 0.03782 | 0.03050 | 0.07315 |
| 1.6 | 0.000000 | 0.07093 | 0.06984 | 0.06877 | 0.06771 | 0.06667 | 0.06564 | 0.06463 | 0.06363 | 0.06264 |
| 1.7 | 0.06167 | 0.06072 | 0.05977 | 0.05884 | 0.05793 | 0.05702 | 0.05613 | 0.05525 | 0.05439 | 0.05354 |
| 1.8 | 0.05270 | 0.05187 | 0.05105 | 0.05025 | 0.04946 | 0.04868 | 0.04791 | 0.04715 | 0.04640 | 0.04567 |
| 1.9 | 0.04494 | 0.04423 | 0.04353 | 0.04284 | 0.04215 | 0.04148 | 0.04082 | 0.04017 | 0.03953 | 0.03890 |
| 2.0 | 0.03828 | 0.03766 | 0.03706 | 0.03647 | 0.03588 | 0.03531 | 0.03474 | 0.03418 | 0.03363 | 0.03309 |
| 2.1 | 0.03256 | 0.03203 | 0.03152 | 0.03101 | 0.03051 | 0.03002 | 0.02953 | 0.02906 | 0.02859 | 0.02813 |
| 2.2 | 0.02767 | 0.02722 | 0.02678 | 0.02635 | 0.02592 | 0.02550 | 0.02509 | 0.02468 | 0.02428 | 0.02389 |
| 2.3 | 0.02350 | 0.02312 | 0.02274 | 0.02237 | 0.02201 | 0.02165 | 0.02130 | 0.02095 | 0.02061 | 0.02028 |
| 2.4 | 0.01995 | 0.01962 | 0.01931 | 0.01899 | 0.01868 | 0.01838 | 0.01808 | 0.01779 | 0.01750 | 0.01721 |
| 2.5 | 0.01693 | 0.01666 | 0.01638 | 0.01612 | 0.01586 | 0.01560 | 0.01534 | 0.01509 | 0.01485 | 0.01461 |
| 2.6 | 0.01437 | 0.01414 | 0.01391 | 0.01368 | 0.01346 | 0.01324 | 0.01302 | 0.01281 | 0.01260 | 0.01240 |
| 2.7 | 0.01220 | 0.01200 | 0.01180 | 0.01161 | 0.01142 | 0.01124 | 0.01106 | 0.01088 | 0.01070 | 0.01053 |
| 2.8 | 0.01036 | 0.01019 | 0.01002 | 0.00986 | 0.00970 | 0.00954 | 0.00939 | 0.00924 | 0.00909 | 0.00894 |
| 2.9 | 0.00880 | 0.00866 | 0.00852 | 0.00838 | 0.00824 | 0.00811 | 0.00/98 | 0.00/85 | 0.00772 | 0.00/60 |
| 3.0 | 0.00/48 | 0.00/30 | 0.00724 | 0.00/12 | 0.00701 | 0.00090 | 0.000/9 | 0.00008 | 0.00037 | 0.00040 |
| 3.1 | 0.00030 | 0.00020 | 0.00010 | 0.00000 | 0.00590 | 0.00587 | 0.00378 | 0.00308 | 0.00339 | 0.00350 |
| 3.3 | 0.00342 | 0.00355 | 0.00324 | 0.00310 | 0.00508 | 0.00426 | 0.00419 | 0.00413 | 0.00476 | 0.00400 |
| 3.4 | 0.00394 | 0.00387 | 0.00381 | 0.00375 | 0.00370 | 0.00364 | 0.00358 | 0.00352 | 0.00347 | 0.00342 |
| 3.5 | 0.00336 | 0.00331 | 0.00326 | 0.00321 | 0.00316 | 0.00311 | 0.00306 | 0.00301 | 0.00297 | 0.00292 |
| 3.6 | 0.00287 | 0.00283 | 0.00279 | 0.00274 | 0.00270 | 0.00266 | 0.00262 | 0.00258 | 0.00254 | 0.00250 |
| 3.7 | 0.00246 | 0.00242 | 0.00239 | 0.00235 | 0.00231 | 0.00228 | 0.00224 | 0.00221 | 0.00217 | 0.00214 |
| 3.8 | 0.00211 | 0.00208 | 0.00204 | 0.00201 | 0.00198 | 0.00195 | 0.00192 | 0.00189 | 0.00187 | 0.00184 |
| 3.9 | 0.00181 | 0.00178 | 0.00176 | 0.00173 | 0.00170 | 0.00168 | 0.00165 | 0.00163 | 0.00160 | 0.00158 |
| 4.0 | 0.00156 | 0.00153 | 0.00151 | 0.00149 | 0.00146 | 0.00144 | 0.00142 | 0.00140 | 0.00138 | 0.00136 |
| 4.1 | 0.00134 | 0.00132 | 0.00130 | 0.00128 | 0.00126 | 0.00124 | 0.00122 | 0.00121 | 0.00119 | 0.00117 |
| 4.2 | 0.00115 | 0.00114 | 0.00112 | 0.00110 | 0.00109 | 0.00107 | 0.00106 | 0.00104 | 0.00102 | 0.00101 |
| 4.3 | 0.00100 | 0.00098 | 0.00097 | 0.00095 | 0.00094 | 0.00093 | 0.00091 | 0.00090 | 0.00089 | 0.00087 |
| 4.4 | 0.00086 | 0.00085 | 0.00084 | 0.00082 | 0.00081 | 0.00080 | 0.00079 | 0.00078 | 0.00077 | 0.00076 |
| 4.5 | 0.00074 | 0.00073 | 0.00072 | 0.00071 | 0.00070 | 0.00069 | 0.00068 | 0.00067 | 0.00066 | 0.00065 |

p-Values for the *t* Distribution – <u>one tail</u>, df = 19

For *two tails*, multiply the value by 2, since the *t* PDF is symmetric. The *p*-value is the colored area under the *t* PDF in the sketch.



Example: 1-tailed *p* at t = 1.06: *p*-value = TDIST(t,df,1) = 0.15122. 2-tailed *p* at t = 1.06: *p*-value = TDIST(t,df,2) = 0.30243.

| t | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
|-----|---------|---------|---------|---------|----------|---------|---------|---------|---------|---------|
| 0.0 | 0.50000 | 0.49606 | 0.49213 | 0.48819 | 0.48426 | 0.48032 | 0.47639 | 0.47246 | 0.46854 | 0.46461 |
| 0.1 | 0.46070 | 0.45678 | 0.45287 | 0.44897 | 0.44507 | 0.44117 | 0.43728 | 0.43340 | 0.42953 | 0.42566 |
| 0.2 | 0.42180 | 0.41795 | 0.41411 | 0.41027 | 0.40645 | 0.40264 | 0.39883 | 0.39504 | 0.39125 | 0.38748 |
| 0.3 | 0.38372 | 0.37997 | 0.37623 | 0.37251 | 0.36879 | 0.36509 | 0.36141 | 0.35774 | 0.35408 | 0.35044 |
| 0.4 | 0.34681 | 0.34320 | 0.33960 | 0.33602 | 0.33245 | 0.32890 | 0.32537 | 0.32185 | 0.31835 | 0.31487 |
| 0.5 | 0.31141 | 0.30796 | 0.30453 | 0.30113 | 0.29774 | 0.29436 | 0.29101 | 0.28768 | 0.28436 | 0.28107 |
| 0.6 | 0.27780 | 0.27454 | 0.27131 | 0.26810 | 0.26491 | 0.26174 | 0.25859 | 0.25546 | 0.25235 | 0.24927 |
| 0.7 | 0.24621 | 0.24316 | 0.24014 | 0.23715 | 0.23417 | 0.23122 | 0.22829 | 0.22538 | 0.22250 | 0.21964 |
| 0.8 | 0.21680 | 0.21398 | 0.21119 | 0.20842 | 0.20008 | 0.20295 | 0.20026 | 0.19/38 | 0.19493 | 0.19230 |
| 1.0 | 0.18909 | 0.18/11 | 0.18433 | 0.18202 | 0.1/931 | 0.17702 | 0.17430 | 0.1/212 | 0.10970 | 0.10/31 |
| 1.0 | 0.10494 | 0.10239 | 0.1002/ | 0.13/9/ | 0.13370 | 0.13343 | 0.13122 | 0.14901 | 0.14085 | 0.14407 |
| 1.1 | 0.14234 | 0.14045 | 0.13834 | 0.13627 | 0.13423 | 0.13221 | 0.13021 | 0.12023 | 0.12028 | 0.12435 |
| 1.3 | 0.12244 | 0.12050 | 0.10126 | 0.09963 | 0.09803 | 0.09644 | 0.09487 | 0.09333 | 0.09181 | 0.09030 |
| 1.4 | 0.08882 | 0.08735 | 0.08590 | 0.08448 | 0.08307 | 0.08168 | 0.08031 | 0.07896 | 0.07763 | 0.07632 |
| 1.5 | 0.07502 | 0.07375 | 0.07249 | 0.07125 | 0.07002 | 0.06882 | 0.06763 | 0.06646 | 0.06531 | 0.06417 |
| 1.6 | 0.06305 | 0.06194 | 0.06086 | 0.05978 | 0.05873 | 0.05769 | 0.05666 | 0.05566 | 0.05466 | 0.05368 |
| 1.7 | 0.05272 | 0.05177 | 0.05084 | 0.04992 | 0.04902 | 0.04813 | 0.04725 | 0.04639 | 0.04554 | 0.04470 |
| 1.8 | 0.04388 | 0.04307 | 0.04228 | 0.04149 | 0.04072 | 0.03996 | 0.03922 | 0.03849 | 0.03777 | 0.03706 |
| 1.9 | 0.03636 | 0.03567 | 0.03500 | 0.03434 | 0.03368 | 0.03304 | 0.03241 | 0.03180 | 0.03119 | 0.03059 |
| 2.0 | 0.03000 | 0.02942 | 0.02886 | 0.02830 | 0.02775 | 0.02721 | 0.02668 | 0.02616 | 0.02565 | 0.02515 |
| 2.1 | 0.02466 | 0.02417 | 0.02370 | 0.02323 | 0.02277 | 0.02232 | 0.02188 | 0.02145 | 0.02102 | 0.02060 |
| 2.2 | 0.02019 | 0.01979 | 0.01939 | 0.01900 | 0.01862 | 0.01825 | 0.01788 | 0.01752 | 0.01716 | 0.01682 |
| 2.3 | 0.01648 | 0.01614 | 0.01581 | 0.01549 | 0.01518 | 0.01487 | 0.01456 | 0.01426 | 0.01397 | 0.01368 |
| 2.4 | 0.01340 | 0.01313 | 0.01286 | 0.01259 | 0.01233 | 0.01207 | 0.01182 | 0.01158 | 0.01134 | 0.01110 |
| 2.5 | 0.01087 | 0.01064 | 0.01042 | 0.01020 | 0.00999 | 0.00978 | 0.00957 | 0.00937 | 0.00918 | 0.00898 |
| 2.0 | 0.008/9 | 0.00861 | 0.00842 | 0.00825 | 0.00807 | 0.00/90 | 0.00//3 | 0.00/5/ | 0.00/41 | 0.00725 |
| 2.7 | 0.00709 | 0.00094 | 0.000/9 | 0.00000 | 0.000001 | 0.00037 | 0.00023 | 0.00010 | 0.00397 | 0.00384 |
| 2.0 | 0.00371 | 0.00339 | 0.00347 | 0.00333 | 0.00323 | 0.00312 | 0.00301 | 0.00490 | 0.00480 | 0.00409 |
| 3.0 | 0.00368 | 0.00360 | 0.00455 | 0.00344 | 0.00420 | 0.00329 | 0.00322 | 0.00315 | 0.00308 | 0.00301 |
| 3.1 | 0.00295 | 0.00288 | 0.00282 | 0.00276 | 0.00270 | 0.00264 | 0.00258 | 0.00252 | 0.00247 | 0.00241 |
| 3.2 | 0.00236 | 0.00230 | 0.00225 | 0.00220 | 0.00215 | 0.00211 | 0.00206 | 0.00201 | 0.00197 | 0.00193 |
| 3.3 | 0.00188 | 0.00184 | 0.00180 | 0.00176 | 0.00172 | 0.00168 | 0.00164 | 0.00161 | 0.00157 | 0.00154 |
| 3.4 | 0.00150 | 0.00147 | 0.00144 | 0.00140 | 0.00137 | 0.00134 | 0.00131 | 0.00128 | 0.00125 | 0.00123 |
| 3.5 | 0.00120 | 0.00117 | 0.00114 | 0.00112 | 0.00109 | 0.00107 | 0.00105 | 0.00102 | 0.00100 | 0.00098 |
| 3.6 | 0.00095 | 0.00093 | 0.00091 | 0.00089 | 0.00087 | 0.00085 | 0.00083 | 0.00081 | 0.00080 | 0.00078 |
| 3.7 | 0.00076 | 0.00074 | 0.00073 | 0.00071 | 0.00069 | 0.00068 | 0.00066 | 0.00065 | 0.00063 | 0.00062 |
| 3.8 | 0.00060 | 0.00059 | 0.00058 | 0.00056 | 0.00055 | 0.00054 | 0.00053 | 0.00052 | 0.00050 | 0.00049 |
| 3.9 | 0.00048 | 0.00047 | 0.00046 | 0.00045 | 0.00044 | 0.00043 | 0.00042 | 0.00041 | 0.00040 | 0.00039 |
| 4.0 | 0.00038 | 0.00037 | 0.00037 | 0.00036 | 0.00035 | 0.00034 | 0.00033 | 0.00033 | 0.00032 | 0.00031 |
| 4.1 | 0.00030 | 0.00030 | 0.00029 | 0.00028 | 0.00028 | 0.00027 | 0.00027 | 0.00026 | 0.00025 | 0.00025 |
| 4.2 | 0.00024 | 0.00024 | 0.00023 | 0.00023 | 0.00022 | 0.00022 | 0.00021 | 0.00021 | 0.00020 | 0.00020 |
| 4.3 | 0.00019 | 0.00019 | 0.00018 | 0.00018 | 0.00018 | 0.00017 | 0.00017 | 0.00010 | 0.00010 | 0.00010 |
| 4.4 | 0.00013 | 0.00013 | 0.00013 | 0.00014 | 0.00014 | 0.00014 | 0.00013 | 0.00013 | 0.00013 | 0.00013 |
| 4.5 | 0.00012 | 0.00012 | 0.00012 | 0.00011 | 0.00011 | 0.00011 | 0.00011 | 0.00010 | 0.00010 | 0.00010 |

p-Values for the *t* Distribution – <u>one tail</u>, df = 29

For *two tails*, multiply the value by 2, since the *t* PDF is symmetric. The *p*-value is the colored area under the *t* PDF in the sketch.



Example: 1-tailed *p* at t = 1.06: *p*-value = TDIST(t,df,1) = 0.14895. 2-tailed *p* at t = 1.06: *p*-value = TDIST(t,df,2) = 0.29789.

| t | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
|-----|---------|---------|----------|---------|---------|---------|---------|---------|---------|---------|
| 0.0 | 0.50000 | 0.49604 | 0.49209 | 0.48814 | 0.48418 | 0.48023 | 0.47628 | 0.47234 | 0.46839 | 0.46445 |
| 0.1 | 0.46052 | 0.45658 | 0.45266 | 0.44873 | 0.44481 | 0.44090 | 0.43700 | 0.43310 | 0.42920 | 0.42532 |
| 0.2 | 0.42144 | 0.41757 | 0.41371 | 0.40985 | 0.40601 | 0.40217 | 0.39835 | 0.39454 | 0.39073 | 0.38694 |
| 0.3 | 0.38316 | 0.37939 | 0.37563 | 0.37189 | 0.36815 | 0.36443 | 0.36073 | 0.35704 | 0.35336 | 0.34969 |
| 0.4 | 0.34604 | 0.34241 | 0.33879 | 0.33519 | 0.33160 | 0.32803 | 0.32447 | 0.32094 | 0.31741 | 0.31391 |
| 0.5 | 0.31042 | 0.30696 | 0.30351 | 0.30007 | 0.29666 | 0.29327 | 0.28989 | 0.28653 | 0.28320 | 0.27988 |
| 0.6 | 0.27658 | 0.27331 | 0.27005 | 0.26681 | 0.26360 | 0.26040 | 0.25723 | 0.25408 | 0.25095 | 0.24784 |
| 0.7 | 0.24475 | 0.24169 | 0.23864 | 0.23562 | 0.23262 | 0.22965 | 0.22669 | 0.22376 | 0.22086 | 0.21797 |
| 0.8 | 0.21511 | 0.2122/ | 0.20945 | 0.20666 | 0.20389 | 0.20114 | 0.19842 | 0.19572 | 0.19305 | 0.19039 |
| 0.9 | 0.18/// | 0.18516 | 0.18238 | 0.18002 | 0.17/49 | 0.17498 | 0.1/250 | 0.17003 | 0.16/60 | 0.16518 |
| 1.0 | 0.102/9 | 0.10042 | 0.12505 | 0.12207 | 0.1334/ | 0.13119 | 0.14895 | 0.14072 | 0.14452 | 0.14234 |
| 1.1 | 0.14019 | 0.13800 | 0.15595 | 0.1558/ | 0.13181 | 0.12977 | 0.12770 | 0.12370 | 0.12579 | 0.12163 |
| 1.2 | 0.11993 | 0.11602 | 0.00050 | 0.00604 | 0.00522 | 0.00373 | 0.10880 | 0.10709 | 0.10555 | 0.10302 |
| 1.5 | 0.08606 | 0.08459 | 0.098313 | 0.09094 | 0.09035 | 0.07889 | 0.07752 | 0.03000 | 0.03307 | 0.03755 |
| 1.5 | 0.07221 | 0.07093 | 0.06967 | 0.06843 | 0.06720 | 0.06599 | 0.06480 | 0.06363 | 0.06248 | 0.06134 |
| 1.6 | 0.06022 | 0.05912 | 0.05803 | 0.05696 | 0.05590 | 0.05487 | 0.05385 | 0.05284 | 0.05185 | 0.05088 |
| 1.7 | 0.04992 | 0.04897 | 0.04804 | 0.04713 | 0.04623 | 0.04535 | 0.04448 | 0.04362 | 0.04278 | 0.04195 |
| 1.8 | 0.04114 | 0.04034 | 0.03955 | 0.03877 | 0.03801 | 0.03726 | 0.03653 | 0.03580 | 0.03509 | 0.03440 |
| 1.9 | 0.03371 | 0.03303 | 0.03237 | 0.03172 | 0.03108 | 0.03045 | 0.02983 | 0.02923 | 0.02863 | 0.02805 |
| 2.0 | 0.02747 | 0.02691 | 0.02635 | 0.02581 | 0.02528 | 0.02475 | 0.02424 | 0.02373 | 0.02324 | 0.02275 |
| 2.1 | 0.02227 | 0.02180 | 0.02134 | 0.02089 | 0.02045 | 0.02001 | 0.01959 | 0.01917 | 0.01876 | 0.01836 |
| 2.2 | 0.01796 | 0.01758 | 0.01720 | 0.01683 | 0.01646 | 0.01610 | 0.01575 | 0.01541 | 0.01507 | 0.01474 |
| 2.3 | 0.01442 | 0.01410 | 0.01379 | 0.01349 | 0.01319 | 0.01290 | 0.01261 | 0.01233 | 0.01205 | 0.01178 |
| 2.4 | 0.01152 | 0.01126 | 0.01101 | 0.01076 | 0.01052 | 0.01028 | 0.01005 | 0.00982 | 0.00960 | 0.00938 |
| 2.5 | 0.00916 | 0.00895 | 0.00875 | 0.00855 | 0.00835 | 0.00816 | 0.00797 | 0.00779 | 0.00761 | 0.00743 |
| 2.6 | 0.00726 | 0.00709 | 0.00692 | 0.00676 | 0.00660 | 0.00645 | 0.00630 | 0.00615 | 0.00600 | 0.00586 |
| 2.7 | 0.00573 | 0.00559 | 0.00546 | 0.00533 | 0.00520 | 0.00508 | 0.00496 | 0.00484 | 0.00472 | 0.00461 |
| 2.8 | 0.00450 | 0.00439 | 0.00429 | 0.00418 | 0.00408 | 0.00398 | 0.00389 | 0.00379 | 0.00370 | 0.00361 |
| 2.9 | 0.00352 | 0.00344 | 0.00333 | 0.00327 | 0.00319 | 0.00311 | 0.00304 | 0.00296 | 0.00289 | 0.00282 |
| 3.0 | 0.00273 | 0.00208 | 0.00202 | 0.00233 | 0.00249 | 0.00243 | 0.00237 | 0.00231 | 0.00225 | 0.00219 |
| 3.1 | 0.00214 | 0.00209 | 0.00203 | 0.00198 | 0.00193 | 0.00188 | 0.00164 | 0.00179 | 0.00175 | 0.00170 |
| 3.3 | 0.00128 | 0.00102 | 0.00122 | 0.00119 | 0.00116 | 0.00140 | 0.00142 | 0.00107 | 0.00103 | 0.00132 |
| 3.4 | 0.00099 | 0.00096 | 0.00094 | 0.00092 | 0.00089 | 0.00087 | 0.00085 | 0.00082 | 0.00080 | 0.00078 |
| 3.5 | 0.00076 | 0.00074 | 0.00072 | 0.00070 | 0.00069 | 0.00067 | 0.00065 | 0.00063 | 0.00062 | 0.00060 |
| 3.6 | 0.00059 | 0.00057 | 0.00056 | 0.00054 | 0.00053 | 0.00051 | 0.00050 | 0.00049 | 0.00047 | 0.00046 |
| 3.7 | 0.00045 | 0.00044 | 0.00043 | 0.00041 | 0.00040 | 0.00039 | 0.00038 | 0.00037 | 0.00036 | 0.00035 |
| 3.8 | 0.00034 | 0.00033 | 0.00033 | 0.00032 | 0.00031 | 0.00030 | 0.00029 | 0.00028 | 0.00028 | 0.00027 |
| 3.9 | 0.00026 | 0.00026 | 0.00025 | 0.00024 | 0.00024 | 0.00023 | 0.00022 | 0.00022 | 0.00021 | 0.00021 |
| 4.0 | 0.00020 | 0.00019 | 0.00019 | 0.00018 | 0.00018 | 0.00017 | 0.00017 | 0.00017 | 0.00016 | 0.00016 |
| 4.1 | 0.00015 | 0.00015 | 0.00014 | 0.00014 | 0.00014 | 0.00013 | 0.00013 | 0.00013 | 0.00012 | 0.00012 |
| 4.2 | 0.00012 | 0.00011 | 0.00011 | 0.00011 | 0.00010 | 0.00010 | 0.00010 | 0.00010 | 0.00009 | 0.00009 |
| 4.3 | 0.00009 | 0.00009 | 0.00008 | 0.00008 | 0.00008 | 0.00008 | 0.00007 | 0.00007 | 0.00007 | 0.00007 |
| 4.4 | 0.00007 | 0.00007 | 0.00006 | 0.00006 | 0.00006 | 0.00006 | 0.00006 | 0.00006 | 0.00005 | 0.00005 |
| 4.5 | 0.00005 | 0.00005 | 0.00005 | 0.00005 | 0.00005 | 0.00004 | 0.00004 | 0.00004 | 0.00004 | 0.00004 |

Folding Diagram for Aliasing Calculations

Instructions for using the folding diagram:

- Calculate the folding frequency, $f_{\text{folding}} = f_s/2$.
- Locate f/f_{folding} on the folding diagram, as plotted below. *Note*: For values of f/f_{folding} greater than 5.0, the folding diagram can easily be extended, following the obvious pattern.
- Read straight down from the value of f/f_{folding} to obtain the value of f_a/f_{folding} on the bottom (horizontal) axis.
- Finally, calculate the aliasing frequency, $f_a =$

$$f_a = \left(\frac{f_a}{f_{\text{folding}}}\right) f_{\text{folding}}$$



Alternative – an equation instead of the folding diagram:

- General equation to determine the perceived frequency of *any* signal frequency *f* when sampled at *any* sampling frequency *f_s*, whether there is aliasing or not: $f_{\text{perceived}} = \left| f f_s \cdot \text{NINT} \left(\frac{f}{f_s} \right) \right|$, where
 - NINT is the "nearest integer" function.
 - In Excel, use ROUND(x,0) to round real number x to the nearest integer.

Thermocouple Voltage Data – Table 9.2 of Wheeler, A. J. and Ganji, A. R., *Introduction to Engineering Experimentation*, Ed. 2, Pearson Education Inc. (Prentice Hall), Upper Saddle River, NJ, 2004.

| IABLE 9.2 | Millivolt Outpu | t of Common | Thermocoupl | es (Reference | e Junction at | :0°C) |
|-----------|-----------------|-------------|-------------|---------------|------------------|--------|
| | ~ <u></u> | | Thermocou | iple type | 1. M | |
| Temperatu | re | | | | | |
| (°C) | Т | E | J | Κ | R | S |
| -250 | -6.181 | -9.719 | | -6.404 | | |
| -200 | -5.603 | -8.824 | -7.890 | -5.891 | | |
| -150 | -4.648 | -7.279 | -6.499 | -4.912 | | |
| -100 | -3.378 | -5.237 | -4.632 | -3.553 | | |
| -50 | -1.819 | -2.787 | -2.431 | -1.889 | | |
| 0 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| 20 | 0.789 | 1.192 | 1.019 | 0.798 | 0.111 | 0.113 |
| 40 | 1.611 | 2.419 | 2.058 | 1.611 | 0.232 | 0.235 |
| 60 | 2.467 | 3.683 | 3.115 | 2.436 | 0.363 | 0.365 |
| 80 | 3.357 | 4.983 | 4.186 | 3.266 | 0.501 | 0.502 |
| 100 | 4.277 | 6.317 | 5.268 | 4.095 | 0.647 | 0.645 |
| 120 | 5.227 | 7.683 | 6.359 | 4.919 | 0.800 | 0.795 |
| 140 | 6.204 | 9.078 | 7.457 | 5.733 | 0.959 | 0.950 |
| 160 | 7.207 | 10.501 | 8.560 | 6.539 | 1.124 | 1.109 |
| 180 | 8.235 | 11.949 | 9.667 | 7.338 | 1.294 | 1.273 |
| 200 | 9.286 | 13.419 | 10.777 | 8.137 | 1.468 | 1.44(|
| 220 | 10.360 | 14.909 | 11.887 | 8.938 | 1.647 | 1.611 |
| 240 | 11.456 | 16.417 | 12.998 | 9.745 | 1.830 | 1.785 |
| 260 | 12.572 | 17.942 | 14.108 | 10.560 | 2.017 | 1.962 |
| 280 | 13.707 | 19.481 | 15.217 | 11.381 | 2.207 | 2.141 |
| 300 | 14.860 | 21.033 | 16.325 | 12.207 | 2.400 | 2.323 |
| 350 | 17.816 | 24.961 | 19.089 | 14.292 | 2.896 | 2.786 |
| 400 | 20.869 | 28.943 | 21.846 | 16.395 | 3.407 | 3.260 |
| 450 | | 32.960 | 24.607 | 18.513 | 3.933 | 3.743 |
| 500 | | 36.999 | 27.388 | 20.640 | 4.471 | 4.234 |
| 600 | | 45.085 | 33.096 | 24.902 | 5.582 | 5.23 |
| 700 | | 53.110 | 39.130 | 29.218 | 6.741 | 6.274 |
| 800 | | 61.022 | | 33.277 | 7.949 | 7.345 |
| 900 | | 68.873 | | 37.325 | 9.203 | 8.448 |
| 1000 | | 76.358 | | 41.269 | 10.503 | 9.585 |
| 1100 | | | | 45.108 | 11.846 | 10.754 |
| 1200 | | | | 48.828 | 13.224 | 11.947 |
| 1300 | | | | 52.398 | 14.624 | 13.155 |
| 1400 | | | | | 16.035 | 14.368 |
| 1500 | | | | | 17.445 | 15.576 |
| 1600 | | | | | 18.842 | 16.771 |
| 1700 | | | | | 20.215 | 17.942 |

Platinum 100-Ω RTD Table

TABLE F.3

Platinum RTD 100 Ω at 0°C, DIN curve 43760, 9–68

| °C | Ohms | °C | Ohms | °C | Ohms | °C | Ohms | °C | Ohms |
|------|-------|-----|--------|-----|--------|-----|--------|-----|--------|
| -200 | 18.53 | -40 | 84.21 | 120 | 146.06 | 280 | 204.88 | 440 | 260.75 |
| -195 | 20.65 | -35 | 86.19 | 125 | 147.94 | 285 | 206.68 | 445 | 262.45 |
| -190 | 22.78 | -30 | 88.17 | 130 | 149.82 | 290 | 208.46 | 450 | 264.14 |
| -185 | 24.92 | -25 | 90.15 | 135 | 151.7 | 295 | 210.25 | 455 | 265.83 |
| -180 | 27.05 | -20 | 92.13 | 140 | 153.57 | 300 | 212.03 | 460 | 267.52 |
| -175 | 29.17 | -15 | 94.1 | 145 | 155.45 | 305 | 213.81 | 465 | 269.21 |
| -170 | 31.28 | -10 | 96.07 | 150 | 157.32 | 310 | 215.58 | 470 | 270.89 |
| -165 | 33.38 | -5 | 98.04 | 155 | 159.18 | 315 | 217.36 | 475 | 272.57 |
| -160 | 35.48 | 0 | 100 | 160 | 161.04 | 320 | 219.13 | 480 | 274.25 |
| -155 | 37.57 | 5 | 101.95 | 165 | 162.9 | 325 | 220.9 | 485 | 275.92 |
| -150 | 39.65 | 10 | 103.9 | 170 | 164.76 | 330 | 222.66 | 490 | 277.6 |
| -145 | 41.73 | 15 | 105.85 | 175 | 166.62 | 335 | 224.42 | 495 | 279.27 |
| -140 | 43.8 | 20 | 107.79 | 180 | 168.47 | 340 | 226.18 | 500 | 280.93 |
| -135 | 45.87 | 25 | 109.73 | 185 | 170.32 | 345 | 227.94 | 505 | 282.6 |
| -130 | 47.93 | 30 | 111.67 | 190 | 172.16 | 350 | 229.69 | 510 | 284.26 |
| -125 | 49.99 | 35 | 113.61 | 195 | 174 | 355 | 231.44 | 515 | 285.91 |
| -120 | 52.04 | 40 | 115.54 | 200 | 175.84 | 360 | 233.19 | 520 | 287.57 |
| -115 | 54.09 | 45 | 117.47 | 205 | 177.68 | 365 | 234.93 | 525 | 289.22 |
| -110 | 56.13 | 50 | 119.4 | 210 | 179.51 | 370 | 236.67 | 530 | 290.87 |
| -105 | 58.17 | 55 | 121.32 | 215 | 181.34 | 375 | 238.41 | 535 | 292.51 |
| -100 | 60.2 | 60 | 123.24 | 220 | 183.17 | 380 | 240.15 | 540 | 294.16 |
| -95 | 62.23 | 65 | 125.16 | 225 | 185 | 385 | 241.88 | 545 | 295.8 |
| -90 | 64.25 | 70 | 127.07 | 230 | 186.82 | 390 | 243.61 | 550 | 297.43 |
| -85 | 66.27 | 75 | 128.98 | 235 | 188.64 | 395 | 245.34 | 555 | 299.07 |
| -80 | 68.28 | 80 | 130.89 | 240 | 190.46 | 400 | 247.06 | 560 | 300.7 |
| -75 | 70.29 | 85 | 132.8 | 245 | 192.27 | 405 | 248.78 | 565 | 302.33 |
| -70 | 72.29 | 90 | 134.7 | 250 | 194.08 | 410 | 250.5 | 570 | 303.95 |
| 65 | 74.29 | 95 | 136.6 | 255 | 195.89 | 415 | 252.21 | 575 | 305.58 |
| -60 | 76.28 | 100 | 138.5 | 260 | 197.7 | 420 | 253.93 | 580 | 307.2 |
| -55 | 78.27 | 105 | 140.39 | 265 | 199.5 | 425 | 255.64 | 585 | 308.81 |
| -50 | 80.25 | 110 | 142.28 | 270 | 201.3 | 430 | 257.34 | 590 | 310.43 |
| -45 | 82.23 | 115 | 144.18 | 275 | 203.09 | 435 | 259.05 | 595 | 312.04 |

(Continued on next page)

(Continued) °C °C Ohms °C Ohms °C Ohms Ohms °C Ohms 600 313.65 655 331.15 710 348.3 765 365.1 820 381.55 605 315.25 660 332.72 715 349.84 770 366.61 825 383.03 610 316.86 334.29 665 720 351.38 775 368.12 830 384.5 615 318.46 670 335.86 725 352.92 780 369.62 835 385.98 620 320.05 675 337.43 730 354.45 785 371.12 840 387.45 625 321.65 680 338.99 735 355.98 790 372.62 845 388.91 630 323.24 685 340.55 740 357.51 795 374.12 850 390.38 635 324.83 690 342.1 745 359.03 800 375.61 640 326.41 695 343.66 750 360.55 805 377.1 645 327.99 700 345.21 755 362.07 810 378.59 650 329.57 705 346.76 760 363.59 815 380.07

 Table taken from R. E. Fraser, Process Measurement and Control – Introduction to Sensors,

 Communication, Adjustment, and Control, Prentice-Hall, Inc., Upper Saddle River, NJ, 2001.

TABLE F.3

| | T (°C) | <i>T</i> (°F) | R (Ω) for type 2252 | R (Ω) for type 5000 |
|---|--------|---------------|---------------------|---------------------|
| t | -10.0 | 14.0 | 12460 | 27670 |
| t | -9.0 | 15.8 | 11810 | 26210 |
| Ī | -8.0 | 17.6 | 11190 | 24830 |
| Ī | -7.0 | 19.4 | 10600 | 23540 |
| Ī | -6.0 | 21.2 | 10050 | 22320 |
| Ī | -5.0 | 23.0 | 9534 | 21170 |
| Ī | -4.0 | 24.8 | 9046 | 20080 |
| Ī | -3.0 | 26.6 | 8586 | 19060 |
| | -2.0 | 28.4 | 8151 | 18100 |
| I | -1.0 | 30.2 | 7741 | 17190 |
| I | 0.0 | 32.0 | 7355 | 16330 |
| | 1.0 | 33.8 | 6989 | 15520 |
| I | 2.0 | 35.6 | 6644 | 14750 |
| | 3.0 | 37.4 | 6319 | 14030 |
| | 4.0 | 39.2 | 6011 | 13340 |
| Ι | 5.0 | 41.0 | 5719 | 12700 |
| | 6.0 | 42.8 | 5444 | 12090 |
| Ι | 7.0 | 44.6 | 5183 | 11510 |
| | 8.0 | 46.4 | 4937 | 10960 |
| | 9.0 | 48.2 | 4703 | 10440 |
| | 10.0 | 50.0 | 4482 | 9951 |
| | 11.0 | 51.8 | 4273 | 9486 |
| | 12.0 | 53.6 | 4074 | 9046 |
| | 13.0 | 55.4 | 3886 | 8628 |
| | 14.0 | 57.2 | 3708 | 8232 |
| | 15.0 | 59.0 | 3539 | 7857 |
| | 16.0 | 60.8 | 3378 | 7500 |
| | 17.0 | 62.6 | 3226 | 7162 |
| l | 18.0 | 64.4 | 3081 | 6841 |
| l | 19.0 | 66.2 | 2944 | 6536 |
| ļ | 20.0 | 68.0 | 2814 | 6247 |
| l | 21.0 | 69.8 | 2690 | 5972 |
| ļ | 22.0 | 71.6 | 2572 | 5710 |
| l | 23.0 | 73.4 | 2460 | 5462 |
| | 24.0 | 75.2 | <u>2354</u> | <u>5225</u> |
| | 25.0 | 77.0 | 2252 | 5000 |
| | 26.0 | 78.8 | 2156 | 4787 |
| | 27.0 | 80.6 | 2064 | 4583 |
| | 28.0 | 82.4 | 1977 | 4389 |
| | 29.0 | 84.2 | 1894 | 4204 |
| | 30.0 | 86.0 | 1815 | 4029 |

Resistance values for two standard thermistors